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SORET EFFECTS DUE TO NATURAL CONVECTION IN A NON-NEWTONIAN FLUID FLOW IN POROUS MEDIUM WITH HEAT AND MASS TRANSFER

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Abstract:

The problem of unsteady MHD free convective, incompressible electrically conducting, non-Newtonian fluid through porous medium bounded by an infinite vertical porous plate in the presence of constant suction has been studied. A magnetic field of uniform strength is assumed to be applied normal to the plate. The equations governing the fluid flow which are highly nonlinear are reduced to linear by using perturbation method and have been solved subject to the relevant boundary conditions. It is noted that the velocity of the fluid is increased as Soret number and suction parameter increase, whereas reverse phenomenon is observed in case of magnetic field strength and sink strength.

Keywords: Non-Newtonian fluid; MHD; Free convection; heat and Mass transfer flow; and suction.

1. Introduction

Magneto hydrodynamics is currently undergoing a period of great enlargement and differentiation of subject matter. Free convection flow occurs frequently in nature, flows of fluid through porous media are of main interest now days and have attracted by many research scholars due to their applications in the science and technology. The study of hydro magnetic convective non-Newtonian fluid flows with heat and mass transfer in porous medium attracted many research due to its applications in many field like, soil physics, geophysics, aerodynamics and aeronautics. The interest in these new problems generates from their importance in liquid metals, electrolytes and ionized gases. Because of their varied importance, these flows have been studied by several authors-notable amongst them are Ferraro and Plumpton (1996) and Crammer and Pai (1973), Pal and Chatterjee (2010), Pal and Talkdar (2010), Chein (2004), Jha and Prasad (1991), Acharya et al. (2000), Kafousias and Raptis (1981), Kishore et al. (2010), Raju et al. (2008 & 2011) . In all the above studies, the fluid models considered are Newtonian. But in view of the mechanism of non-Newtonian flows, which are used in various manufacturing processes, play a very important role in industrial applications and modern technology. Many authors like Choudary and Das (2013), Emmanuel and Khan (2006), Rafeal (2007), and Rushikumar and Sivaraj (2012), Hayat et al. (2010). Kelly et al. (1999), Reddy et al. (2010), investigated an unsteady free convective MHD non-Newtonian flow through a porous medium bounded by an infinite inclined porous plate. Motivated by the above cited work, in this paper, we consider an unsteady MHD free convective, thermal diffusive and viscos-elastic fluid with heat and mass transfer in porous medium bounded by an infinite vertical porous plate with heat absorption and viscous dissipation.

2. Mathematical Formulation

We consider a two-dimensional unsteady MHD free convection non-Newtonian mass transfer flow of an incompressible viscous fluid with and suction past an infinite vertical porous plate. In rectangular Cartesian coordinate system, we take x^1 -axis along the infinite plate in the direction of flow and y^1 -axis normal to it. All the fluid properties are constant except the density in the buoyancy force term. The Eckert number *Ec* and the magnetic Reynolds number *Rm* are small, so that the induced magnetic field can be neglected.

The governing equations for continuity, momentum, energy and concentration take the following form:

$$
\frac{\partial v^1}{\partial y^1} = 0\tag{1}
$$

$$
\frac{\partial u^1}{\partial t^1} + v^1 \frac{\partial u^1}{\partial y^1} = g\beta (T^1 - T_\infty) + g\beta^1 (C^1 - C_\infty) + v \frac{\partial^2 u^1}{\partial y^1} + B_1 \left(\frac{\partial^3 u^1}{\partial t^1 \partial y^1} + v^1 \frac{\partial^3 u^1}{\partial y^1} \right) - \frac{\partial B_0^2}{\rho} u^1 - \frac{v}{k} u^1 \tag{2}
$$

$$
\frac{\partial T^1}{\partial t^1} + v^1 \frac{\partial T^1}{\partial y^1} = \frac{K_T}{\rho C_p} \frac{\partial^2 T^1}{\partial y^1^2} + A^1 (T^1 - T_\infty) + \frac{\nu}{C_p} \left(\frac{\partial u^1}{\partial y^1}\right)^2 \tag{3}
$$

$$
\frac{\partial C^1}{\partial t^1} + v^1 \frac{\partial C^1}{\partial y^1} = D \frac{\partial^2 C^1}{\partial y^1^2} + D_1 \frac{\partial^2 T^1}{\partial y^1^2}
$$
\n(4)

The boundary conditions relevant to the problem are;

$$
u^{1} = 0, v^{1} = -v_{0}, T^{1} = T_{w} + \varepsilon (T_{w} - T_{\infty})e^{i\omega t}, C^{1} = C_{w} + \varepsilon (C_{w} - C_{\infty})e^{i\omega t} \text{ at } y^{1} = 0
$$

\n
$$
u^{1} \to 0, T^{1} \to T_{\infty}, C^{1} \to C_{\infty} \text{ as } y^{1} \to \infty
$$
\n(5)

Where u^1 the dimensional velocity component, T^1 the dimensional temperature distribution, C^1 the dimensional concentration distribution, T_{∞}^1 dimensional temperature far away from the plate, C_{∞}^1 dimensional concentration far away from the plate, T_w temperature near the plate, C_w concentration near the plate, t^1 dimensional time, x^1 *y 1* dimensional Cartesian coordinates along and normal to the plate, *B⁰* transverse magnetic field, *g* is the acceleration due to gravity, v^I dimensional suction velocity, B_I kinematical non-Newtonian parameter, k is the permeability of the porous medium, *β* volumetric expansion coefficient, *β 1* volumetric expansion coefficient of mass diffusion, θ kinematic viscosity, ρ is the density of the fluid, σ electrical conductivity, K_T thermal mass dirtusion, θ kinematic viscosity, ρ is the density of the full σ electrical conductivity, K_T thermal
conductivity, ε is a perturbation parameter (<<1), c_p is specific heat, A^T is heat absorption c

On introducing the following non-dimensional quantities,

conductivity,
$$
\varepsilon
$$
 is a perturbation parameter ($\langle < 1 \rangle$, c_p is specific heat, A' is heat absorption coefficient, ω is
frequency parameter, D is mass diffusivity, and D_I thermal diffusivity.
On introducing the following non-dimensional quantities,
 $y = \frac{y^1 v_0}{v}, u = \frac{u^1}{v_0}, t = \frac{t^1 v_0^2}{4v}, T = \frac{T^1 - T_\infty}{T_\infty - T_\infty}, v = \frac{\mu}{\rho}, A = \frac{A^1 v_0^2}{4v}, R_m = \frac{B_1 v_0^2}{v^2}, C = \frac{C^1 - C_\infty}{C_\infty - C_\infty}, G_r = \frac{g \beta v (T_w - T_\infty)}{v_0^3},$

$$
G_m = \frac{g \beta^1 v (C_w - C_\infty)}{v_0^3}, M = \frac{\sigma v B_0^2}{\rho v_0^2}, K = \frac{v^2 k}{v_0^2}, P_r = \frac{v \rho C_p}{K_T}, E_c = \frac{v_0^2}{C_p (T_w - T_\infty)},
$$
(6)

$$
S_c = \frac{v}{D}, S_0 = \frac{D_1}{v} \left(\frac{T_w - T_\infty}{C_w - C_\infty} \right)
$$
in set of Equations (2) . (4) we obtain the governing equations in the dimensionless form as

in set of Equations (2)- (4), we obtain the governing equations in the dimensionless form as

$$
\frac{1}{4}\frac{\partial u}{\partial t} - \frac{\partial u}{\partial y} = G_r T + G_m C + \frac{\partial^2 u}{\partial y^2} + R_m \left(\frac{1}{4}\frac{\partial^3 u}{\partial t \partial y^2} - \frac{\partial^3 u}{\partial y^3}\right) - M_1 u \tag{7}
$$

$$
\frac{P_r}{4} \frac{\partial T}{\partial t} - P_r \frac{\partial T}{\partial y} = \frac{\partial^2 T}{\partial y^2} + \frac{AP_r}{4} T + P_r E_c \left(\frac{\partial u}{\partial y}\right)^2
$$
\n(8)

$$
\frac{1}{4}\frac{\partial C}{\partial t} - \frac{\partial C}{\partial y} = \frac{1}{S_c}\frac{\partial^2 C}{\partial y^2} + S_0 \left(\frac{\partial^2 T}{\partial y^2}\right)
$$
\n(9)

 $M_1 = M + 1/K$, *Gr* is Grashof's number, *Gm* is modified Grashof's number, R_m is dimensionless no-Newtonian parameter, *M* the magnetic parameter, and *K* is permeability parameter, *Pr* Prandtl number, *Ec* is Eckert number, *Sc* Schmidt number, and S_0 is Soret number. Now the boundary conditions (4) reduce into the following form

$$
u = 0, \t T = 1 + \varepsilon e^{i\omega t}, \t C = 1 + \varepsilon e^{i\omega t} \t at \t y = 0\n u \to 0, \t T \to 0, \t C \to 0 \t as \t y \to \infty \t (10)
$$

3. Solution of the Problem

To solve the partial differential equations (6) , (7) , (8) subject to the boundary conditions (9) , the velocity (u) , the temperature (T) and the concentration (C) in the neighborhood of the plate are assumed to be of the form;

$$
u(y,t) = f_0(y) + \varepsilon e^{i\omega t} f_1(y) = f_0 + \varepsilon e^{i\omega t} f_1
$$
\n(11)

$$
u(y,t) = f_0(y) + \varepsilon e \t f_1(y) = f_0 + \varepsilon e \t f_1
$$

\n
$$
T(y,t) = g_0(y) + \varepsilon e^{i\omega t} g_1(y) = g_0 + \varepsilon e^{i\omega t} g_1
$$
\n(12)

$$
T(y,t) = g_0(y) + \varepsilon e^{-\varepsilon t} g_1(y) = g_0 + \varepsilon e^{-\varepsilon t} g_1
$$

\n
$$
C(y,t) = h_0(y) + \varepsilon e^{i\omega t} h_1(y) = h_0 + \varepsilon e^{i\omega t} h_1
$$
\n(13)

Substituting Equations (11), (12), (13) in Equations (7), (8), (9) and equating the coefficients of ε^0 , ε^1

(neglecting
$$
\varepsilon^2
$$
 terms etc.), we obtain the following set of ordinary differential equations.
\n
$$
R_m f_0^{111} - f_0^{11} - f_0^{11} + M_1 f_0 = G_r g_0 + G_m h_0
$$
\n(14)

$$
R_m f_0^{111} - f_0^{11} - f_0^{1} + M_1 f_0 = G_r g_0 + G_m h_0
$$
\n
$$
R_m f_1^{111} - \left(1 + \frac{R_m i\omega}{4}\right) f_1^{11} - f_1^{1} + \left(M_1 + \frac{i\omega}{4}\right) f_1 = G_r g_1 + G_m h_1
$$
\n(15)

$$
g_0^{11} + P_r g_0^1 + \frac{AP_r}{4} g_0 = -P_r E_c (f_0^1)^2
$$
\n(16)

$$
g_1^{11} + P_r g_1^1 + \frac{P_r}{4} (A - i\omega) g_1 = -2P_r E_c f_0^1 f_1^1
$$
\n(17)

$$
h_0^{11} + S_c h_0^{1} = -S_0 S_c g_0^{11}
$$

\n
$$
h_0^{11} + S_h h_0^{1} - \frac{S_c i \omega}{2} h_0 = -S_0 S_e g_0^{11}
$$
 (19)

$$
h_1^{11} + S_c h_1^1 - \frac{S_c l \omega}{4} h_1 = -S_0 S_c g_1^{11}
$$

And the corresponding boundary conditions are

 $u_0 = u_1 = 0$, $T_0 = T_1 = 1$, $C_0 = C_1 = 1$ at $y = 0$ $u_0, u_1 \to 0,$ $T_0, T_1 \to 0,$ $C_0, C_1 \to 0$ as $y \to \infty$ (20)

In Equations (14) and (15), due to presence of elasticity, we get $3rd$ order differential equations. To solve these differential equations we need three boundary conditions, but we have only two. So we assume the solutions as;

$$
f_0 = f_{00} + R_m f_{01} \qquad g_0 = g_{00} + R_m g_{01} \qquad h_0 = h_{00} + R_m h_{01} f_1 = f_{10} + R_m f_{11} \qquad g_1 = g_{10} + R_m g_{11} \qquad h_1 = h_{10} + R_m h_{11} \qquad (21)
$$

Substitute Equations (21) in the Equations (14), (15), (16), (17), (18), (19), equating the coefficients of R_m^0 , R_m^{-1} (neglecting higher order terms), we obtain the following set of ordinary differential equations. **Zero order:**

$$
f_{00}^{11} + f_{00}^{1} - M_1 f_{00} = -G_r g_{00} - G_m h_{00}
$$
 (22)

$$
f_{10}^{11} + f_{10}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{10} = -G_r g_{10} - G_m h_{10}
$$
\n(23)

$$
g_{00}^{11} + P_r g_{00}^{1} + \frac{AP_r}{4} g_{00} = -P_r E_c (f_{00}^{1})^2
$$
\n(24)

$$
g_{10}^{11} + P_r g_{10}^{1} + \frac{P_r}{4} (A - i\omega) g_{10} = -P_r E_c f_{00}^{1} f_{10}^{1}
$$
\n(24)

$$
h_{00}^{11} + S_c h_{00}^{1} = -S_0 S_c g_{00}^{11}
$$
 (26)

$$
h_{10}^{11} + S_c h_{10}^{1} - \frac{S_c i \omega}{4} h_{10} = -S_0 S_c g_{10}^{11}
$$
\n(27)

First order:

$$
f_{01}^{11} + f_{01}^{1} - M_1 f_{01} = f_{00}^{111} - G_r g_{01} - G_m h_{01}
$$

\n
$$
f_{11}^{11} + f_{11}^{1} - \left(M_1 + \frac{i\omega}{r}\right) f_{11} = f_{10}^{111} - \frac{i\omega}{r}\n f_{10}^{11} - G_r g_{11} - G_m h_{11}
$$
\n(28)

$$
f_{11}^{11} + f_{11}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{11} = f_{10}^{111} - \frac{i\omega}{4} f_{10}^{11} - G_r g_{11} - G_m h_{11}
$$
\n(29)

$$
g_{01}^{11} + P_r g_{01}^{1} + \frac{AP_r}{4} g_{01} = -2P_r E_c f_{00}^{1} f_{01}^{1}
$$
\n(30)

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$$
g_{11}^{11} + P_r g_{11}^{1} + \frac{P_r}{4} (A - i\omega) g_{11} = -2P_r E_c \left(f_{00}^{11} f_{11}^{11} + f_{01}^{11} f_{10}^{11} \right)
$$
\n(31)

$$
h_{01}^{11} + S_c h_{01}^{1} = -S_0 S_c g_{01}^{11}
$$
\n(32)

$$
h_{11}^{11} + S_c h_{11}^{1} - \frac{S_c i \omega}{4} h_{11} = -S_0 S_c g_{11}^{11}
$$
\n(33)

In order to solve the above non-linear system of equations (22) to (33), expand f_{00} , f_{01} , f_{10} , f_{11} , g_{00} , g_{01} , g_{10} , g_{11} , h_{00} , h_{01} , h_{10} , h_{11} in powers of Eckert number (E_c < < 1) for all incompressible fluids. So, we assume that

$$
f_{00} = f_{000} + E_c f_{001} + o(E_c^2) \t g_{00} = g_{000} + E_c g_{001} + o(E_c^2) \t h_{00} = h_{000} + E_c h_{001} + o(E_c^2)
$$

\n
$$
f_{01} = f_{010} + E_c f_{011} + o(E_c^2) \t g_{01} = g_{010} + E_c g_{011} + o(E_c^2) \t h_{01} = h_{010} + E_c h_{011} + o(E_c^2)
$$

\n
$$
f_{10} = f_{100} + E_c f_{101} + o(E_c^2) \t g_{10} = g_{100} + E_c g_{101} + o(E_c^2) \t h_{10} = h_{100} + E_c h_{101} + o(E_c^2)
$$

\n
$$
f_{11} = f_{110} + E_c f_{111} + o(E_c^2) \t g_{11} = g_{110} + E_c g_{111} + o(E_c^2) \t h_{11} = h_{110} + E_c h_{111} + o(E_c^2) \t (34)
$$

Using Equations (34) in Equations (22) to (33) and equating the coefficients of E_c^0 , E_c^1 (neglecting the coefficients of E_c^2 etc.,), we get the following set of differential equations;

Zero order terms:

$$
f_{000}^{11} + f_{000}^{1} - M_1 f_{000} = -G_r g_{000} - G_m h_{000}
$$
\n(35)

$$
f_{000}^{11} + f_{000}^{1} - M_1 f_{000} = -G_r g_{000} - G_m h_{000}
$$
\n
$$
f_{100}^{11} + f_{100}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{100} = -G_r g_{100} - G_m h_{100}
$$
\n(36)

$$
g_{000}^{11} + P_r g_{000}^{1} + \frac{AP_r}{4} g_{000} = 0
$$
\n(37)

$$
g_{100}^{11} + P_r g_{100}^{1} + \frac{P_r}{4} (A - i\omega) g_{100} = 0
$$
\n(38)

$$
h_{000}^{11} + S_c h_{000}^{1} = -S_0 S_c g_{000}^{11}
$$
\n(39)

$$
h_{100}^{11} + S_c h_{100}^{1} - \frac{S_c i \omega}{4} h_{100} = -S_0 S_c g_{100}^{11}
$$
\n(40)

(40)
\n
$$
f_{010}^{11} + f_{010}^{1} - M_1 f_{010} = f_{000}^{111} - G_r g_{010} - G_m h_{010}
$$
\n
$$
f_{110}^{11} + f_{110}^{11} - \left(M_1 + \frac{i\omega}{L}\right) f_{110} = f_{100}^{111} - \frac{i\omega}{L}\left(f_{100}^{11} - G_r g_{110} - G_m h_{110}\right)
$$
\n(41)

$$
f_{110}^{11} + f_{110}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{110} = f_{100}^{111} - \frac{i\omega}{4} f_{100}^{11} - G_r g_{110} - G_m h_{110}
$$
\n(42)

$$
g_{010}^{11} + P_r g_{010}^1 + \frac{AP_r}{4} g_{010} = 0
$$
\n(43)

$$
g_{110}^{11} + P_r g_{110}^{1} + \frac{P_r}{4} (A - i\omega) g_{110} = 0
$$
\n(44)

$$
h_{010}^{11} + S_c h_{010}^{1} = -S_0 S_c g_{010}^{11}
$$
\n(45)

$$
h_{110}^{11} + S_c h_{110}^{1} - \frac{S_c i \omega}{4} h_{110} = -S_0 S_c g_{110}^{11}
$$
\n
$$
(46)
$$

First order terms:

$$
f_{001}^{11} + f_{001}^{1} - M_1 f_{001} = -G_r g_{001} - G_m h_{001}
$$
\n(47)

$$
f_{101}^{11} + f_{101}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{101} = -G_r g_{101} - G_m h_{101}
$$
\n(48)

$$
g_{001}^{11} + P_r g_{001}^{1} + \frac{AP_r}{4} g_{001} = -P_r f_{000}^{1^2}
$$
\n(49)

$$
g_{101}^{11} + P_r g_{101}^{1} + \frac{P_r}{4} (A - i\omega) g_{101} = -P_r f_{000}^{1} f_{100}^{1}
$$
\n(49)

$$
h_{001}^{11} + S_c h_{001}^{1} = -S_0 S_c g_{001}^{11}
$$
\n(51)

$$
h_{101}^{11} + S_c h_{101}^{1} - \frac{S_c i \omega}{4} h_{101} = -S_0 S_c g_{101}^{11}
$$
\n(52)

(52)
\n
$$
f_{011}^{11} + f_{011}^{1} - M_1 f_{011} = f_{001}^{111} - G_r g_{011} - G_m h_{011}
$$
\n
$$
f_{111}^{11} + f_{111}^{1} - \left(M_1 + \frac{i\omega}{\omega}\right) f_{111} = f_{101}^{111} - \frac{i\omega}{\omega} f_{101}^{11} - G_r g_{111} - G_m h_{111}
$$

$$
f_{111}^{11} + f_{111}^{1} - \left(M_1 + \frac{i\omega}{4}\right) f_{111} = f_{101}^{111} - \frac{i\omega}{4} f_{101}^{11} - G_r g_{111} - G_m h_{111}
$$
\n(54)

$$
g_{011}^{11} + P_r g_{011}^{1} + \frac{AP_r}{4} g_{011} = -2P_r f_{000}^{1} f_{010}^{1}
$$
\n(55)

$$
g_{111}^{11} + P_r g_{111}^{1} + \frac{P_r}{4} (A - i\omega) g_{111} = -2P_r \left(f_{000}^{1} f_{110}^{1} + f_{010}^{1} f_{100}^{1} \right)
$$
\n(55)

$$
h_{011}^{11} + S_c h_{011}^{1} = -S_0 S_c g_{011}^{11}
$$
\n(57)

$$
h_{111}^{11} + S_c h_{111}^{1} - \frac{S_c i \omega}{4} h_{111} = -S_0 S_c g_{111}^{11}
$$
\n(58)

And the boundary conditions (20) reduce to

$$
f_{000} = f_{010} = f_{001} = f_{011} = f_{100} = f_{110} = f_{101} = f_{111} = 0
$$

\n
$$
g_{000} = 1, g_{010} = g_{001} = g_{011} = 0, g_{100} = 1, g_{110} = g_{101} = g_{111} = 0
$$

\n
$$
h_{000} = 1, h_{010} = h_{001} = h_{011} = 0, h_{100} = 1, h_{110} = h_{101} = h_{111} = 0
$$

\n
$$
f_{000} \rightarrow f_{010} \rightarrow f_{001} \rightarrow f_{011} \rightarrow f_{100} \rightarrow f_{110} \rightarrow f_{101} \rightarrow f_{111} \rightarrow 0
$$

\n
$$
g_{000} \rightarrow g_{010} \rightarrow g_{001} \rightarrow g_{011} \rightarrow g_{100} \rightarrow g_{110} \rightarrow g_{101} \rightarrow g_{111} \rightarrow 0
$$

\n
$$
h_{000} \rightarrow h_{010} \rightarrow h_{001} \rightarrow h_{011} \rightarrow h_{100} \rightarrow h_{110} \rightarrow h_{101} \rightarrow h_{111} \rightarrow 0
$$

\nAs $y \rightarrow \infty$ (59)

Solving these differential equations (35) to (58), using the above boundary conditions, also making use of Equations (34) and the approximate substitutions in Equations (21), we obtain velocity (*u*), temperature (*T*) and concentration (*C*).

Skin-Friction:

The expression for the skin-friction (τ) at the plate is,

$$
\tau = \left(\frac{du}{dy}\right)_{y=0} = \left(\frac{df_0}{dy}\right)_{y=0} + \varepsilon e^{i\omega t} \left(\frac{df_1}{dy}\right)_{y=0} = A_{165} + \varepsilon e^{i\omega t} A_{166}
$$
\n(60)

Rate of heat transfer:

The expression for the rate of heat transfer in terms of Nusselt number (N_u) is,

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$$
N_u = \left(\frac{dT}{dy}\right)_{y=0} = \left(\frac{dg_0}{dy}\right)_{y=0} + \varepsilon e^{i\omega t} \left(\frac{dg_1}{dy}\right)_{y=0} = A_{167} + \varepsilon e^{i\omega t} A_{168}
$$
(61)

Rate of mass transfer:

The expression for the rate of mass transfer in the form of Sherwood number (S_h) is,

$$
S_h = \left(\frac{dC}{dy}\right)_{y=0} = \left(\frac{dh_0}{dy}\right)_{y=0} + \varepsilon e^{i\omega t} \left(\frac{dh_1}{dy}\right)_{y=0} = A_{169} + \varepsilon e^{i\omega t} A_{170}
$$
(62)

6. Results and Discussion

In order to get physical insight into the problem, the velocity, the temperature, the concentration, skin friction, rate of heat transfer and rate of mass transfer have been discussed by assigning numerical values for M, Pr, and A while keeping Rm=0.05, w=5.0, e=2.0, Ec=0.001. Velocity profiles are displayed in Figs. 1-3, with the variations in the physical parameters like magnetic parameter M, sink parameter A, and Soret number So. We have choose Pr=0.025 and 1.0 which represent mercury and electrolytic solution respectively. For the validity of our results, we compared our results with the data sets of Reddy et al. [15] at the absence of mass transfer. From this it is noticed that our results are in good agreement with the existing results (see Fig. 9). In Fig. 1 the effects of magnetic parameter M on velocity is presented. From this figure it is noticed that velocity decreases as magnetic parameter M increases. So it indicates that external magnetic field that acts as Lorentz's force which suppresses the free convection. The effect of thermal diffusion on velocity is presented in Fig. 2, it is noticed that velocity increases as Soret number So increases as expected. In Fig. 3 velocity profiles are presented with the variations in sink parameter A, we observe that velocity increases as sink parameter A increases. In the Figs. 4-7, variations in temperature distribution are presented for various values of sink parameter A, soret number So, Schmidt number Sc and magnetic parameter M. From these figures it is interesting to notice that, temperature decreases with the increase in suction parameter A, soret number So, Schmidt number Sc respectively, where as it shows reverse action in the case of magnetic parameter M. Similarly, the effects of soret number So on concentration are presented in Fig. 8, the concentration decreases as soret number So increases. Therefore, we have noticed that Velocity and Temperature are greater for mercury than that of electrolytic solution. From Table 1, it can be observed that skin friction increases with an increase in Hartmann number where as it shows reverse effect in the case of Grashof's number, modified Grashof's number, dimensionless non Newtonian parameter and permeability parameter. From Table 2, it is noticed that rate of heat transfer decreases with an increase in the sink strength. From Table 3, we see that rate of mass transfer also decreases with an increase in thermal diffusion number.

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Fig. 5: Effects of Soret number on Temperature Fig. 6: Effects of M on Temperature

Fig. 3: Effects of Suction parameter on velocity Fig. 4: Effects of Suction parameter on Temperature

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Pr	Ec	\mathbf{A}	Nu
0.71	0.1	0.1	-2.6694
0.74	0.1	0.1	-3.0096
0.77	0.1	0.1	-3.4449
0.71	0.2	0.1	-1.0678
0.71	0.3	0.1	-2.4025
0.71	0.1	0.2	-3.3648
0.71	0.1	0.3	-3.9998

Table 1: Variations in rate of heat transfer

Fig. 9: Effects of *M* on velocity at the absence of *Sc* and *S0*

7. Conclusion

In this paper, the effect of unsteady free convective MHD non-Newtonian flow through a porous medium with suction bounded by an infinite porous plate has been studied numerically. Neglecting the induced magnetic field, the equations governing the velocity, the temperature and the concentration of the fluid are solved by multi-parameter perturbation technique in terms of dimensionless parameters. The conclusions are summarized as follows: External magnetic field suppresses the free convection flow. The velocity for viscous fluid is more than that of viscos-elastic fluids. The temperature of the fluid is more for mercury than for an electrolytic solution. Skin friction increases with an increase in permeability of porous medium and Hartmann number. Rate of heat transfer decreases with an increase in the sink strength and rate of mass transfer also decreases with an increase in thermal diffusion number.

Gr	Gm	Rm	$\overline{\mathbf{K}}$	M	τ
5	5	0.1	0.6	2	-2.9074
10	5	0.1	0.6	2	-5.1735
15	5	0.1	0.6	2	-7.7128
5	10	0.1	0.6	2	-1.5082
5	15	0.1	0.6	2	-4.2167
5	5	0.2	0.6	2	-5.8149
5	5	0.3	0.6	2	-8.7223
5	5	0.1	0.7	2	-2.8623
5	5	0.1	0.8	2	-1.1020
5	5	0.1	0.6	3	-3.0838
5	5	0.1	0.6	$\overline{4}$	-2.6694

Table 2: Variations in Skin-friction Table 3: Variations in rate of mass transfer

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